

# Maths Calculation Policy

September 2019

Objective & Strategy	Concrete	Pictorial	Abstract	
Combining two parts to make a whole: part- whole model	Use part part whole model. Use cubes to add two num-bers together as a group or in a bar.	3 Balls 2 Ball	4 + 3 = 7 $5$ $3$ $10 = 6 + 4$ Use the part-part whole diagram as shown above to move into the abstract.	
Starting at the big- ger number and counting on	Start with the larger number on the bead string and then count on to the smaller num- ber 1 by 1 to find the answer.	12 + 5 = 17 10 11 12 13 14 15 16 17 18 19 20 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.	
Regrouping to make 10. This is an essential skill for column addition later.	6+5=11 Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10. 9 + 5 = 14	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?	
Represent & use number bonds and related subtraction facts within 20	2 more than 5.	$\begin{array}{c c} & & & \\ \hline \\ & & & \\ \hline \\ \hline$	Emphasis should be on the language '1 more than 5 is equal to 6.' '2 more than 5 is 7.' '8 is 3 more than 5.'	

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Adding multiples of ten	50= 30 = 20		20 + 30 = 50 70 = 50 + 20	
	Model using dienes and bead strings	3 tens + 5 tens = tens 30 + 50 = Use representations for base ten.	40 + 🗆 = 60	
Use known number facts Part part whole	20 Children ex- plore ways of making num- bers within 20	20 < =	+ 1 = 16 $16 - 1 =1 + = 16 $ $16 - = 1$	
Using known facts	<sup>L</sup> LL + <sup>L</sup> LL = <sup>L</sup> LLLLL	$\begin{array}{cccc} \cdot & + & \cdot \\ & + & \cdot \\ & & $	3 + 4 = 7 leads to 30 + 40 = 70 leads to 300 + 400 = 700	
Bar model		7 + 3 = 10	<b>23 25</b> <b>?</b> 23 + 25 = 48	

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Add a two digit number and ones	17 + 5 = 22         Use ten frame to make 'magic ten         Children explore the pattern.         17 + 5 = 22         27 + 5 = 32	Use part part whole and number line to model. 17 + 5 = 22 (3 (2) 16 + 7 (20) 16 + 7 (16) (16) (2) (2) (16) (2) (16) (2) (16) (2) (16) (2) (16) (2) (16) (16) (16) (16) (16) (16) (16) (16	17 + 5 = 22 Explore related facts $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $17 - 5$ $22 - 5 = 17$	
Add a 2 digit num- ber and tens	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 	27 + 10 = 37 27 + 20 = 47 27 + □ = 57	
Add two 2-digit numbers	Model using dienes , place value counters and numicon	+20 +5 Or +20 +3 +2 47 $67$ $72$ $47$ $67$ $70$ $72Use number line and bridge ten using partwhole if necessary.$	25 + 47 $20 + 5$ $40 + 7$ $20 + 40 = 60$ $5 + 7 = 12$ $60 + 12 = 72$	
Add three 1-digit numbers	Combine to make 10 first if possible, or bridge 10 then add third digit	Regroup and draw representation. + $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$	4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make/bridge ten then add on the third.	





Objective & Strategy	Concrete	Pictorial	Abstract	
Taking away ones.	Use physical objects, counters, cubes etc to show how objects can be taken away. 6-4=2 4-2=2	$\begin{array}{c} & & & & & & \\ & & & & & & \\ & & & & & $	7—4 = 3 16—9 = 7	2
Counting back	Move objects away from the group, counting backwards. Move the beads along the bead string as you count backwards.	$\begin{array}{c c} -1 & -1 & -1 \\ \hline & 5 & -3 & = 2 \\ \hline & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline \end{array}$ Count back in ones using a number line.	Put 13 in your head, count back 4. What number are you at?	
Find the Difference	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I am 2 years older than my sister' 5 Pencils 3 Erasers 2 Lay objects to represent bar model.	Count on using a number line to find the difference. *6 $+6$ $0$ $1$ $2$ $3$ $4$ $5$ $6$ $7$ $8$ $9$ $10$ $11$ $12$	Hannah has12 sweets and her sister has 5. How many more does Hannah have than her sister.?	

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Represent and use number bonds and related subtraction facts within 20 Part Part Whole model	Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the arts, what s the other part?		Move to using numbers within the part whole model.	y y
	10—6 = 4	Use pictorial representations to show the part.		
Make 10	14—9	13 - 7 $13 - 7 = 6$ $3 - 4$ $4 - 4$	16—8 How many do we take off first to get to 10? How many left to take off?	
Bar model	<b>5−2 = 3</b>		8 2 10 = 8 + 2 10 = 2 + 8 10-2 = 8	
			10—8 = 2	

<b>Objective &amp; Strategy</b>	Concrete	Pictorial	Abstract	
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'	20 - 4 =	20—4 = 16	<b>X</b> 2
Partitioning to sub- tract without re- grouping. 'Friendly numbers'	34-13 = 21 Use Dienes to show how to par- tition the number when subtracting without regroup- ing.	Children draw representations of Dienes and cross off.	43—21 = 22	UBTR
Make ten strategy Progression should be crossing one ten, crossing more than one ten, cross- ing the hundreds.	34-28 Use a bead bar or bead strings to model counting to next ten and the rest.	$\begin{array}{c} & & & \\ \hline \hline & & & \\ \hline & & \hline \\ \hline & & & \\ \hline & & & \\ \hline \hline & & & \\ \hline \hline & & & \\ \hline \hline \\ \hline & & & \\ \hline \hline \\ \hline & & & \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \\ \hline \hline$	93—76 = 17	<b>CTO</b>
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Objective &	Concrete	Pictorial	Abstract	
Strategy				
Column subtraction without regrouping (friendly numbers)	47—32	$\begin{array}{c} \hline \\ \hline $	47 - 24 = 23 $-\frac{40 + 7}{20 + 4}$ -20 + 3	λ3
	Use base 10 or Numicon to model	Darw representations to support under- standing	Intermediate step may be needed to lead to clear subtraction under- standing.	2
Column subtraction with regrouping	Tens ones	45 -29 Tens lones 16 HIL 200 200	$\begin{array}{r} 8 \ 36 \ -25 \ 4^{=} \ 582 \\ \hline 300 \ 130 \ 6 \\ - \ 200 \ 50 \ 4 \\ \hline 500 \ 80 \ 2 \end{array} \end{array} Begin by partitioning into pv columns$	
	Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange.	Children may draw base ten or PV counters and cross off.	728-582=146       Then move to $\overset{\mu}{\cancel{7}}$ 128 $\overset{\mu}{\cancel{7}}$ 128 $582$ 146         146       146	R

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Subtracting tens and ones Year 4 subtract with up to 4 digits. Introduce decimal subtrac- tion through context of money	234 - 179 234 - 179 234 - 179	Children to draw pv counters and show their exchange—see Y3	2 x 5 4 - 1 5 6 2 1 1 9 2 Use the phrase 'take and make' for ex- change	SUB
Year 5- Subtract with at least 4 dig- its, including money and measures. Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal	As Year 4	Children to draw pv counters and show their exchange—see Y3	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	TRAC
Year 6—Subtract with increasingly large and more complex numbers and decimal values.			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Doubling	Use practical activities using manip- ultives including cubes and Numicon to demonstrate doubling + = = + = = double 4 is 8 $4 \times 2 = 8$ + = = =	Draw pictures to show how to double numbers	Partition a number and then double each part before recombining it back together. 16 10 10 10 10 10 10 10 10 12 12 = 32	
Counting in multi- ples	Count the groups as children are skip counting, children may use their fin- gers as they are skip counting.	Children make representations to show counting in multiples. $2 \begin{array}{c} 2 \\ 2 \\ 4 \end{array} \begin{array}{c} 2 \\ 4 \end{array} \begin{array}{c} 2 \\ 6 \end{array} \begin{array}{c} 2 \end{array} \begin{array}{c} 2 \end{array} \begin{array}{c} 2 \\ 6 \end{array} \begin{array}{c} 2 \end{array} \end{array} \begin{array}{c} 2 \end{array} \begin{array}{c} 2 \end{array} \end{array} \end{array} \begin{array}{c} 2 \end{array} \end{array} \begin{array}{c} 2 \end{array} \end{array} \end{array} $ \end{array}  \end{array}	Count in multiples of a number aloud. Write sequences with multiples of num- bers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25 , 30	PLCAT
Making equal groups and counting the total	Use manipulatives to create equal groups.	Draw to show 2 x 3 = 6 Draw and make representations	2 x 4 = 8	<b>N</b>

#### Cliffe VC Primary School Calculation Policy

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Repeated addition	Use different objects to add equal groups	Use pictorial including number lines to solve prob How many sweets are in 5 bags altogether?	Write addition sentences to describe objects and pictures. $\underbrace{\begin{array}{c} \hline \\ \hline $	
Understanding ar- rays	Use objects laid out in arrays to find the an- swers to 2 lots 5, 3 lots of 2 etc.	Draw representations of arrays to show under- standing	3 x 2 = 6 2 x 5 = 10	PLCAT

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Doubling	Model doubling using dienes and PV counters.	Draw pictures and representations to show how to double numbers	Partition a number and then double each part before recombining it back together. 16 10 10 10 10 10 10 10 12 12 = 32	
	40 + 12 = 52			
Counting in multi- ples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fin- gers as they are skip counting. Use bar models. 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40	Number lines, counting sticks and bar models should be used to show repre- sentation of counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15	
	IIII     IIII     IIII     IIII       ?	3 3 3 3 ?	0, 5, 10, 15, 20, 25 , 30 4 × 3 =	

Objective &	Concrete	Pictorial	Abstract	
Strategy				
Multiplication is commutative	Create arrays using counters and cubes and Numicon.	Use representations of arrays to show different calculations and explore commutativity.	$12 = 3 \times 4$ $12 = 4 \times 3$ Use an array to write multiplication sentences and reinforce repeated addition. $00000$ $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$	
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.		$\begin{vmatrix} 4 & 2 \\ \hline 4 & 2 \\ \hline \times & = \\ \hline \times & = \\ \hline \times & = \\ \hline \div & = \\ \hline \div & = \\ \hline \div & = \\ \end{vmatrix}$	2 x 4 = 8 4 x 2 = 8 8 $\div$ 2 = 4 8 $\div$ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 $\div$ 4 4 = 8 $\div$ 2 Show all 8 related fact family sentences.	CATION X







Objective &	Concrete	Pictorial	Abstract	
Strategy				
Multiplying decimals			Remind children that the single digit belongs	
es by a single digit.			points in the question and the answer.	
			3.10	
			x x x	
			25.52	

#### Cliffe VC Primary School Calculation Policy



Objective &	Concrete	Pictorial	Abstract	
Strategy				
Division as sharing	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quanti- ties. 3 + 2 = 4 Children use bar modelling to show and support understanding. 12 12 + 4 = 3	12÷3=4	
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping $ \begin{array}{c} +3 & +3 & +3 & +3 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ \hline 0 & 1 & 2 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 10 & 11 & 12 & 10 & 10$	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?	

Objective &	Concrete	Pictorial	Abstract
Strategy			
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding. 24 divided into groups of $6 = 4$ $96 \div 3 = 32$	Continue to use bar modelling to aid solving division problems. 20 20 $\div$ 5 = ? 5 x ? = 20	How many groups of 6 in 24? 24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$ $28 = 7 \times 4$ $28 = 4 \times 7$ $4 = 28 \div 7$ $7 = 28 \div 4$







### Long Division

2

Step 1 continued...



When dividing the ones, 4 goes into 7 one time. Multiply  $1 \times 4 = 4$ , write that four under the 7, and subract. This finds us the remainder of 3.

Check: 4 × 61 + 3 = 247



When dividing the ones, 4 goes into 9 two times. Multiply  $2 \times 4 = 8$ , write that eight under the 9, and subract. This finds us the remainder of 1.

Check: 4 × 402 + 1 = 1,609

## Long Division

Step 2—a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o <mark>2</mark> 2 ) <mark>5</mark> 8	t o 2 2 ) <u>5</u> 8 - 4 1	t ∘ 2 9 2 ) 5 <mark>8</mark> -4↓ 1 <mark>8</mark>
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens but there is a remainder!	To find it, multiply $2 \times 2 = 4$ , write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o	t o
2 9 2 ) 5 8	29	2)58
<u>-4</u>	$-\frac{4}{10}$	$-\frac{4}{10}$
<mark>  0</mark>	- <u>18</u>	<u>- 1 8</u>
	<mark>0</mark>	0
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.



